Search

Finding Solutions in Life since Brutus

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Mathematical Proof

Search
Uninformed Search
Informed Search

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Proof

- Series of steps that logically follow from step to conclusion
- Showing validity
- To disprove, just show counterexample

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Enumeration

- "Brute Force"
- Just list every possibility
- Obviously only applies to finite, enumerable sets
- Useful for certain applications, like logic (truth tables)

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Direct

- Start with premises, and get to goal
- For equivalence, remember to prove both ways

Proof by Contradiction

- Prove that the opposite of our statement is false
- · Assume goal is false
- Prove a contradiction
- We essentially used this when doing automated logical resolution
- Examples
 - Infinitude of Primes
 - Sqrt(2) is irrational

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Induction

- "Recursion in math"
- Requires partial ordering (ordered, and bounded at one end)
- Example
 - -0+1+...+n = n(n+1)/2

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Mathematical Proof
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Search

- High-level definition: Examining future options to determine what immediate action should be taken
- Assumptions
 - Environment Observable (not hidden)
 - Environment known
 - Deterministic actions

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Problem Formulations

- States
- Initial State
- Actions
- Transition Model
- Goal Test
- Path Cost
 - Step Cost

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Search

- Better definition: Looking for a *sequence of actions* to take that achieves the *goal*. That sequence of actions is called the *solution*.
- Initial State, actions, transition model are, together, called the *state space*.
 - All reachable states from the initial state
- All state spaces can be represented as a graph

Search Terminology

- Incremental (start with nothing, and add states)
- Complete-state (start with everything) and rearrange, or delete

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Search Tree

- All searches can be represented as a search tree of nodes
- Nodes are not states. Nodes represent a state in the search
- Expanding nodes
- Leaf nodes of search together, is the frontier
- Can keep explored set to not visit repeat.

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General Graph Search

- See Russell/Norvig figure 3.7
- Different searches all about how you choose next leaf to expand.
- Nodes need to store
 - Corresponding state
 - Parent
 - Action taken by parent to get here
 - Path Cost (g(n))

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Breath-First Search (BFS)

- Choose next node by putting nodes in Queue
- Ignores all costs

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Depth-First Search (DFS)

• Replace the queue in BFS with a stack

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Uniform-Cost Search

- Also called Dijkstra's Algorithm
- Expand node with lowest g(n)

Iterative Deepening DFS

- Go one layer at a time, doing DFS every time
- Repeats nodes

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Bidirectional Search

- Start search from both start and goal.
- This works because if *e* is avg number of edges at a node,
 - $-e^t$ nodes expanded in t steps.
 - If 2<e, then $2(e^t) < e(e^t)$

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Informed Search

- Uses a heuristic function, h(n)
 - Intuition about the world
 - Estimated cost of cheapest path from the state at node n to goal
 - − Let C=g+h
 - h*=oracle heuristic
 - $-C^* = Optimlal cost$

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Detour: Distance

- *d* is a distance iff *d*:X,Y->**R**, s.t.
 - -d(p,q) >= 0
 - -d(p,q) = 0 iff p=q
 - -d(p,q) = d(q,p) Commutativity
 - $-d(p,q) \le d(p,r) + d(r,q)$ Triangle Inequality

Detour: Distance

- Euclidean Distances
 - Square roots of sum of squares (L₂ norm)
 - Manhattan distance (Lo norm)
 - $-L_{inf}$ norm (Chebyshev distance) = $max_i(abs(p_i q_i))$
- Non-Euclidean
 - Hamming distance
 - Edit distance
 - Cosine distance
 - Jaccard distance

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Evaluation

- Completeness: Will check all nodes to find solution
- Optimality: The solution returned will be optimal
- Optimally Efficient: For another algorithm using same cost function and same heuristic, you cannot expand fewer nodes.

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Best-First Search

- Give every node an f(n) to calculate a priority.
- Pick the one with the best priority
- With uniform cost search, notice f(n)=g(n)
- Greedy Best-first search
 - Intuition: Expand node closest to goal
 - Complete: Yes
 - Optimal: No

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A* Search

- Set f(n) = g(n) + h(n)
- Intuitively, f(n) is estimated cost from initial state to goal through the current node
- Conditions
 - -h(n) must be admissible heuristic
 - Consistency (monotonicity)
 - $-h(n) \ll c(n,a,n')+h(n')$

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A*

- Optimal
- Complete
- Optimally Efficient
- However, can be costly

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Alternatives

- IDA* (Iterative Deepening A*)
- RFBS (Recursive BFS)
- SMA (Simple Memory-Bounded A*)

Search

- Domination
 - For any node n, if $h_2 >= h_1$ then h_2 dominates h_1 .
 - Since we can't pass C*, dominant heuristics are good
 - A weak heuristic takes us closer to uniform-cost search
- Generating heuristics
 - Multiple heuristics: can take $max\{h_1, h_2, h_3, ...\}$
 - Cost of optimal solution to a relaxed problem is an admissible heuristic fo the original problem

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